

## EXPLICIT FINITE DIFFERENCE APPROXIMATION

Take the simplified pressure equation:

$$\left(\frac{\partial P}{\partial t}\right) = \frac{k}{c\phi\mu} \left(\frac{\partial^2 P}{\partial x^2}\right)$$

where the constant  $\frac{k}{c\phi\mu}$  is the hydraulic diffusivity. We can denote this by  $D_h$ .  
If we assume  $D_h = 1$  we get the equation:

$$\left(\frac{\partial P}{\partial t}\right) = \left(\frac{\partial^2 P}{\partial x^2}\right)$$

→ This is the pressure equation for a 1D system.

To continue with the finite difference approximation we must:

1. Discretise the  $x$ -direction by dividing it into a numerical gridblock of size  $\Delta x$
2. Choose a time step,  $\Delta t$
3. Use the following notation:

$P_i^n$  → time level  $n=0,1,2$   
→  $x$ -grid block label,  $i=1,2,3 \dots N_x$  (at  $x=L$ )

$P_i^n$  current (known)  $P$  at time level  
 $P_i^{n+1}$  is the new (unknown)  $P$  at time level.

4. Fix the boundary conditions (for this case are):

$P_1 = P_{in}$  and  $P_{N_x} = P_{out} = P_o$  which are fixed for all of  $t$ .

5. Apply finite differences to obtain:

$$\left(\frac{\partial P}{\partial t}\right)_i \approx \frac{P_i^{n+1} - P_i^n}{\Delta t}$$